

1. Schreibe mittels binomische Formeln als Summe!

- a) $(2a + 3b)^2 = \underline{4a^2 + 12ab + 9b^2}$
 b) $(4x + \frac{3}{2}y)^2 = \underline{16x^2 + 12xy + \frac{9}{4}y^2}$
 c) $(\frac{3}{2}u - \frac{2}{3}v)^2 = \underline{\frac{9}{4}u^2 - 2uv + \frac{4}{9}v^2}$
 d) $(\frac{5}{3}a + \frac{3}{4}b) \cdot (\frac{5}{3}a - \frac{3}{4}b) = \underline{\frac{25}{9}a^2 - \frac{9}{16}b^2}$
 e) $((3x - \frac{5}{2}) \cdot (3x + \frac{5}{2}))^2 = (9x^2 - \frac{25}{4})^2 = \underline{81x^4 - \frac{225}{2}x^2 + \frac{625}{16}}$

2. Wandle folgende Summen in Produkte um!

- a) $81a^2 + 36ab + 4b^2 = \underline{(9a + 2b)^2}$
 b) $\frac{4}{49}x^2 + \frac{16}{7}xy + 16y^2 = \underline{(\frac{2}{7}x + 4y)^2}$
 c) $\frac{1}{100}s^2 - \frac{8}{15}s + \frac{64}{9} = \underline{(\frac{1}{10}s - \frac{8}{3})^2}$
 d) $\frac{25}{16} - 100t^2 = \underline{(\frac{5}{4} + 10t) \cdot (\frac{5}{4} - 10t)}$
 e) $\frac{1}{4}x^2 - 10 = \underline{(\frac{1}{2}x + \sqrt{10}) \cdot (\frac{1}{2}x - \sqrt{10})}$

3. Vereinfache folgende Brüche!

- a) $\frac{9a^2 - 16b^2}{3a - 4b} = \frac{(3a + 4b) \cdot (3a - 4b)}{3a - 4b} = \underline{3a + 4b}$
 b) $\frac{0,01 - 100t^2}{10t + 0,1} = \frac{(0,1 + 10t) \cdot (0,1 - 10t)}{0,1 + 10t} = \underline{0,1 - 10t}$
 c) $\frac{144u^2 - 0,25}{0,5 - 12u} = \frac{(12u + 0,5) \cdot (12u - 0,5)}{-(12u - 0,5)} = \underline{-12u - 0,5}$
 d) $\frac{121v^2 - 8,8v + 0,16}{121v^2 + 8,8v + 0,16} = \frac{(11v - 0,4)^2}{(11v + 0,4)^2} = \underline{\left(\frac{11v - 0,4}{11v + 0,4}\right)^2}$
 e) $\frac{0,18 - 50x^2}{0,6 + 10x} = \frac{2 \cdot (0,09 - 25x^2)}{2 \cdot (0,3 + 5x)} = \frac{(0,3 + 5x) \cdot (0,3 - 5x)}{0,3 + 5x} = \underline{0,3 - 5x}$

4. Löse folgende quadratische Gleichungen mittels binomischer Formeln!

- a) $100x^2 + 10x + \frac{1}{4} = 0 \rightarrow (10x + \frac{1}{2})^2 = 0 \rightarrow \underline{x = -\frac{1}{20}}$
 b) $4x^2 - \frac{16}{3}x + \frac{16}{9} = 0 \rightarrow (2x - \frac{4}{3})^2 = 0 \rightarrow \underline{x = \frac{2}{3}}$
 c) $x^2 - \frac{3}{4} = 0 \rightarrow (x + \sqrt{\frac{3}{4}}) \cdot (x - \sqrt{\frac{3}{4}}) = 0 \rightarrow \underline{x_1 = -\frac{1}{2}\sqrt{3}} \quad \underline{x_2 = \frac{1}{2}\sqrt{3}}$