

1. $f(x) = 5\sqrt{13-3x} - 10$

$D_f: 13-3x \geq 0 \rightarrow 13 \geq 3x \quad | :3$

$\rightarrow x \leq \frac{13}{3} \rightarrow D_f = \{x \mid x \leq \frac{13}{3}; x \in \mathbb{R}\}$

Nullstellen: $5\sqrt{13-3x} - 10 = 0 \rightarrow 5\sqrt{13-3x} = 10 \quad | :5 \rightarrow \sqrt{13-3x} = 2 \quad | \text{Quadrieren}$

$\rightarrow 13-3x = 4 \rightarrow x = 3$

Probe: $5\sqrt{13-9} - 10 = 0$ wahre Aussage

\rightarrow **Nullstelle** $x_0 = 3$

2. $f(x) = 3\sqrt{x+1} - \sqrt{9x-2} - 1$

$D_f: x \geq -1$ und $x \geq \frac{2}{9} \rightarrow D_f = \{x \mid x \geq \frac{2}{9}; x \in \mathbb{R}\}$

Nullstellen: $3\sqrt{x+1} - \sqrt{9x-2} - 1 = 0 \rightarrow 3\sqrt{x+1} = \sqrt{9x-2} + 1 \quad | \text{Quadrieren}$

$\rightarrow 9(x+1) = 9x-2 + 2\sqrt{9x-2} + 1 \rightarrow 9x+9 = 9x-1 + 2\sqrt{9x-2} \quad | -9x+1$

$\rightarrow 10 = 2\sqrt{9x-2} \quad | :2 \rightarrow 5 = \sqrt{9x-2} \quad | \text{Quadrieren}$

$\rightarrow 25 = 9x-2 \rightarrow x = 3$

Probe: $3\sqrt{3+1} - \sqrt{27-2} - 1 = 0$ wahre Aussage

\rightarrow **Nullstelle** $x_0 = 3$

3. $f(x) = \sqrt{x-3} + \sqrt{x+3} - \sqrt{2x}$

$D_f: x \geq 3$ und $x \geq -3$ und $x \geq 0 \rightarrow D_f = \{x \mid x \geq 3; x \in \mathbb{R}\}$

Nullstellen: $\rightarrow \sqrt{x-3} + \sqrt{x+3} - \sqrt{2x} = 0 \quad | +\sqrt{2x} \rightarrow \sqrt{x-3} + \sqrt{x+3} = \sqrt{2x} \quad | \text{Quadrieren}$

$\rightarrow x-3 + 2\sqrt{(x-3)(x+3)} + x+3 = 2x \quad | -2x$

$\rightarrow 2\sqrt{x^2-9} = 0 \quad | \text{Quadrieren} \rightarrow x^2 = 9$

$\rightarrow x_1 = 3 \quad [x_2 = -3]$ entfällt, da $-3 \notin D_f$

Probe: $\sqrt{3-3} + \sqrt{3+3} - \sqrt{6} = 0$ wahre Aussage

\rightarrow **Nullstelle** $x_0 = 3$

4. $f(x) = \sqrt{6x+13} + \sqrt{9x-2} - \sqrt{50x-19}$

$D_f: D_f = \{x \mid x \geq \frac{19}{50}; x \in \mathbb{R}\}$

Nullstellen: $\sqrt{6x+13} + \sqrt{9x-2} - \sqrt{50x-19} = 0 \quad | +\sqrt{50x-19}$

$\sqrt{6x+13} + \sqrt{9x-2} = \sqrt{50x-19} \quad | \text{Quadrieren}$

$6x+13 + 2\sqrt{(6x+13)(9x-2)} + 9x-2 = 50x-19 \quad | -15x-11$

$2\sqrt{(6x+13)(9x-2)} = 35x-30 \quad | \text{Quadrieren}$

$4(6x+13)(9x-2) = 1225x^2 - 2100x + 900$

$216x^2 - 48x + 468x - 104 = 1225x^2 - 2100x + 900 \quad | -216x^2 - 420x + 104$

$1009x^2 - 2520x + 1004 = 0 \quad | :1009$

$x^2 - \frac{2520}{1009}x + \frac{1004}{1009} = 0$

$x_{1,2} = \frac{1260}{1009} \pm \sqrt{\frac{1587600}{1009^2} - \frac{1013036}{1009^2}}$

$x_{1,2} = \frac{1260}{1009} \pm \sqrt{\frac{574564}{1009^2}} \rightarrow x_{1,2} = \frac{1260}{1009} \pm \frac{758}{1009} \rightarrow x_1 = \frac{2018}{1009} = 2 \quad x_2 = \frac{502}{1009} \approx 0,4975$

Nullstelle: $x_0 = 2 \quad (x_0 \approx 0,4975 \text{ entfällt, da Scheinlösung})$

5. $f(x) = \sqrt{9+4x} + \sqrt{4-x} - \sqrt{6x+1}$

$D_f: D_f = \{x \mid -\frac{1}{6} \leq x \leq 4; x \in \mathbb{R}\}$

Nullstelle: $x_0 = 4 \quad (x_0 = 0 \text{ entfällt, da Scheinlösung})$

6. $f(x) = \sqrt{x-10} - \sqrt{x-2} - \sqrt{x-7} + \sqrt{x+5}$

$D_f: D_f = \{x \mid 10 \leq x; x \in \mathbb{R}\}$

Nullstelle: $x_0 = 11$