

1. $f(x) = 2\sin^2 x - 5\sqrt{2}\sin x + 4$

$$\rightarrow 2\sin^2 x - 5\sqrt{2}\sin x + 4 = 0 \quad | : 2 \rightarrow \sin^2 x - \frac{5}{2}\sqrt{2}\sin x + 2 = 0$$

$$\text{Subst.: } z = \sin x \rightarrow z^2 - \frac{5}{2}\sqrt{2}z + 2 = 0 \rightarrow z_{1,2} = \frac{5}{4}\sqrt{2} \pm \sqrt{\frac{25}{8} - \frac{16}{8}} = \frac{5}{4}\sqrt{2} \pm \frac{3}{4}\sqrt{2}$$

$$\rightarrow z_1 = 2\sqrt{2} \text{ oder } z_2 = \frac{1}{2}\sqrt{2} \rightarrow \text{Rücksubstitution: } \sin x = 2\sqrt{2} \text{ oder } \sin x = \frac{1}{2}\sqrt{2}$$

$\rightarrow \sin x = 2\sqrt{2}$ hat keine Lösungen

$$\rightarrow \text{Nullstellen: } \underline{x_{01} = \frac{\pi}{4} + 2k\pi} \quad \underline{x_{02} = \frac{3}{4}\pi + 2k\pi}$$

2. $f(x) = 4\cos(2x-1) - 2$

$$\rightarrow 4\cos(2x-1) - 2 = 0 \quad | : 4 \rightarrow \cos(2x-1) = \frac{1}{2}$$

$$\rightarrow 2x-1 = \frac{\pi}{3} + 2k\pi \text{ oder } 2x-1 = \frac{5}{3}\pi + 2k\pi$$

$$\rightarrow \text{Nullstellen: } \underline{x_{01} = \frac{1}{2} + \frac{\pi}{6} + k\pi \approx 1,02 + k\pi} \quad \underline{x_{02} = \frac{1}{2} + \frac{5}{6}\pi + k\pi \approx 3,12 + k\pi}$$

3. $f(x) = 3\sin x - \cos x - 3$

$$\rightarrow 3\sin x - \cos x - 3 = 0 \rightarrow \text{Subst.: } \boxed{\cos x = \sqrt{1 - \sin^2 x}}$$

$$\rightarrow 3\sin x - \sqrt{1 - \sin^2 x} - 3 = 0 \quad | +\sqrt{1 - \sin^2 x} \rightarrow 3\sin x - 3 = \sqrt{1 - \sin^2 x} \quad | \text{Quadrieren}$$

$$\rightarrow 9\sin^2 x - 18\sin x + 9 = 1 - \sin^2 x \quad | -1 + \sin^2 x \rightarrow 10\sin^2 x - 18\sin x + 8 = 0 \quad | : 10$$

$$\rightarrow \sin^2 x - 1,8\sin x + 0,8 = 0 \rightarrow \text{Subst.: } z = \sin x$$

$$\rightarrow z^2 - 1,8z + 0,8 = 0 \rightarrow z_1 = 1 \text{ oder } z_2 = 0,8 \rightarrow \text{Rücksubstitution: } \sin x = 1 \text{ oder } \sin x = 0,8$$

$$\rightarrow x_1 = \frac{\pi}{2} + 2k\pi \quad x_2 \approx 0,927 + 2k\pi \quad x_3 \approx 2,214 + 2k\pi$$

$$\rightarrow \text{Probe: für } \frac{\pi}{2} \rightarrow 3\sin\frac{\pi}{2} - \cos\frac{\pi}{2} - 3 = 0 \rightarrow 3 - 0 - 3 = 0 \text{ wahre Aussage}$$

$$\text{für } 0,927 \rightarrow 3\sin 0,927 - \cos 0,927 - 3 = 0 \rightarrow 2,4 - 0,6 - 3 = 0 \text{ falsche Aussage}$$

$$\text{für } 2,214 \rightarrow 3\sin 2,214 - \cos 2,214 - 3 = 0 \rightarrow 2,4 + 0,6 - 3 = 0 \text{ wahre Aussage}$$

$$\rightarrow \text{Nullstellen: } \underline{x_{01} = \frac{\pi}{2} + 2k\pi} \quad \underline{x_{02} \approx 2,214 + 2k\pi}$$

4. $f(x) = 2\cos 2x - 2\sin x$

$$\rightarrow 2\cos 2x - 2\sin x = 0 \quad | : 2 \rightarrow \cos 2x - \sin x = 0 \rightarrow \text{Subst.: } \boxed{\cos 2x = 1 - 2\sin^2 x}$$

$$\rightarrow 1 - 2\sin^2 x - \sin x = 0 \rightarrow \text{Subst.: } z = \sin x \rightarrow z^2 + \frac{1}{2}z - \frac{1}{2} = 0$$

$$\rightarrow z_1 = \frac{1}{2} \text{ oder } z_2 = -1 \rightarrow \text{Rücksubstitution: } \sin x = \frac{1}{2} \text{ oder } \sin x = -1$$

$$\rightarrow x_1 = \frac{\pi}{6} + 2k\pi \quad x_2 = \frac{5}{6}\pi + 2k\pi \quad x_3 = \frac{3}{2}\pi + 2k\pi$$

$$\rightarrow \text{Probe: für } \frac{\pi}{6} \rightarrow 2\cos\frac{\pi}{3} - 2\sin\frac{\pi}{6} = 0 \rightarrow 1 - 1 = 0 \text{ wahre Aussage}$$

$$\text{für } \frac{5}{6}\pi \rightarrow 2\cos\frac{5}{3}\pi - 2\sin\frac{5}{6}\pi = 0 \rightarrow -1 - 1 = 0 \text{ falsche Aussage!!!}$$

$$\text{für } \frac{3}{2}\pi \rightarrow 2\cos 3\pi - 2\sin\frac{3}{2}\pi = 0 \rightarrow -2 + 2 = 0 \text{ wahre Aussage}$$

$$\rightarrow \text{Nullstellen: } \underline{x_{01} = \frac{\pi}{6} + 2k\pi} \quad \underline{x_{02} = \frac{3}{2}\pi + 2k\pi}$$